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*Aligns to the  
Common Core  
State Standards*

# Strategies for Teaching **FRACTIONS**

Using Error Analysis for  
Intervention and Assessment

**David B. Spangler**





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Acquisitions Editor: Jessica Allan  
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Typesetter: C&M Digitals (P) Ltd.  
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Cover Designer: Anthony Paular  
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Printed in the United States of America

*Library of Congress Cataloging-in-Publication Data*

Spangler, David B.

Strategies for teaching fractions : using error analysis for intervention and assessment / David B. Spangler.

p. cm.  
Includes bibliographical references.

ISBN 978-1-4129-9398-2 (pbk.)

1. Fractions—Study and teaching. 2. Error analysis (Mathematics) I. Title.

QA137.S73 2011  
372.7'2—dc23      2011019155

This book is printed on acid-free paper.

11 12 13 14 15 1 2 3 4 5 6 7 8 9 10

# Contents

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<b>Preface</b>	<b>ix</b>
<b>Acknowledgments</b>	<b>xv</b>
<b>About the Author</b>	<b>xvii</b>
<b>A Look at the Academic Research: Intervention in the Mathematics Classroom</b>	<b>1</b>
Introduction to the Academic Research	2
Equity and Accessing Language	3
Student Dispositions	4
Activating Prior Knowledge	5
Representations	5
Estimation and Mental Math	7
Alternative Algorithms	8
Differentiating Instruction	9
Instructional Games and Technology	11
Response to Intervention	12
The Teaching of Fractions	13
<i>Questions for Teacher Reflection</i>	19
<b>Big Ideas in Fractions and Problem Solving</b>	<b>21</b>
Fraction Concepts and Fraction Computation	22
Actions and Operations: Problem Structures for Addition, Subtraction, Multiplication, and Division	24
<i>Questions for Teacher Reflection</i>	33
<b>Unit 1: Fraction Concepts</b>	<b>35</b>
Diagnostic Test	36
Item Analysis for Diagnostic Test	39
Error Patterns & Intervention Activities	42
Practice Exercises	86
<i>Questions for Teacher Reflection</i>	88
<b>Unit 2: Addition/Subtraction of Fractions and Mixed Numbers</b>	<b>89</b>
Diagnostic Test	90
Item Analysis for Diagnostic Test	92

Error Patterns & Intervention Activities	95
Practice Exercises	117
<i>Questions for Teacher Reflection</i>	118
<b>Unit 3: Multiplication/Division of Fractions and Mixed Numbers</b>	<b>119</b>
Diagnostic Test	120
Item Analysis for Diagnostic Test	122
Error Patterns & Intervention Activities	125
Practice Exercises	155
<i>Questions for Teacher Reflection</i>	156
<b>Resources: Worksheets, Activities, and Instructional Games (Blacklines)</b>	<b>157</b>
<b>Resources for Fraction Concepts</b>	<b>159</b>
Number Lines (marked 0 to 1)	160
Number Lines (marked beyond 1)	161
Activity: Multiples in <i>Motion</i>	162
Unit Wholes (length model)	163
Instructional Game: Equivalent Fractions Cover-All	164
Activity: Fraction Card Match	166
Benchmark Fractions	167
Activity: Paper-Folding to Find Fraction/Decimal Equivalents	168
<b>Resources for Addition/Subtraction of Fractions and Mixed Numbers</b>	<b>171</b>
Instructional Game: Fractions on My Plate	172
Using Benchmarks to Estimate Sums and Differences	180
Activity Lesson: Making <i>Sum Difference</i> Using Strips to Add/Subtract Fractions	181
Activity Lesson: Adding Probabilities	183
Editor Error Search (+/-)	185
Instructional Game: Rolling <i>a-Plot</i> of Fractions	186
<b>Resources for Multiplication/Division of Fractions and Mixed Numbers</b>	<b>189</b>
Activity Lesson: <i>It's in the Fold</i> : Introduction to Multiplying Fractions	190
Estimating Products Using Benchmarks, Rounding, and Compatible Numbers	195
Activity Lesson: Probability of Successive Events	196
Activity Lesson: How Many Strips Will Fit? Introduction to Dividing Fractions	198
Instructional Game: Balance the Number Sentence!	202
Estimating Quotients Using Benchmarks, Rounding, and Compatible Numbers	206
Editor Error Search ( $\times/\div$ )	207

<b>Answers for Student Materials</b>	<b>209</b>
Answers for Unit 1: Fraction Concepts	209
Answers for Unit 2: Addition/Subtraction of Fractions and Mixed Numbers	211
Answers for Unit 3: Multiplication/Division of Fractions and Mixed Numbers	214
<b>References</b>	<b>219</b>
<b>Technology Resources Online</b>	<b>225</b>